

## Math

1.

To understand the academic performance of 1,000 students, the systematic sampling method is adopted to choose 40 samples. What should the sampling interval be?

2.

A tetrahedron's edge length is  $\sqrt{2}$  and its four points are on a sphere, so what is the sphere's area?

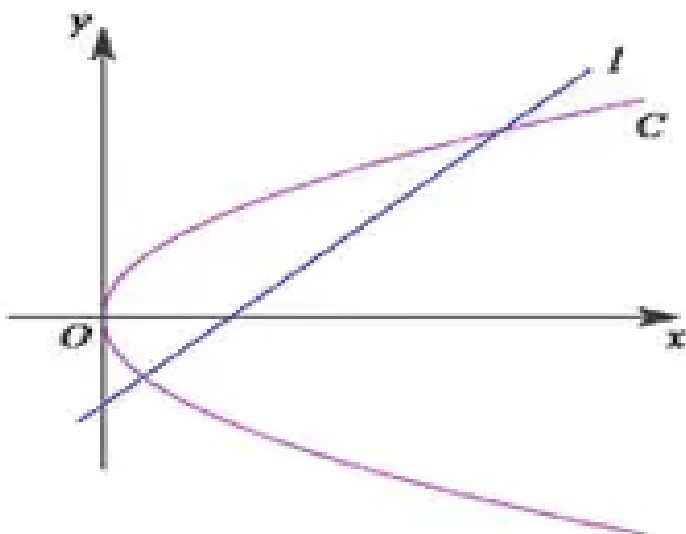
3.

Given  $f(x) = \sin x - (2\sqrt{3}) (\sin^2(\pi/2))$ :

A) Find  $f(x)$ 's smallest positive revolution

B) Find  $f(x)$ 's smallest value, given that the period is  $[0, 2\pi/3]$

4.



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As illustrated in the figure above, in the frame  $xOy$ , we have a line  $l: x-y-2=0$  and a parabola  $C: y^2=2px (p>0)$

I) If  $l$  passes through the focus of the parabola  $C$ , find the equation of the parabola.

II) Given that there are two different points  $P$  and  $Q$  that is symmetrical about line  $l$

1) Prove that the coordinates of the middle point of the line segment  $PQ$  is  $(2-p, -p)$

2) Find the range of  $p$ .

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## 5.

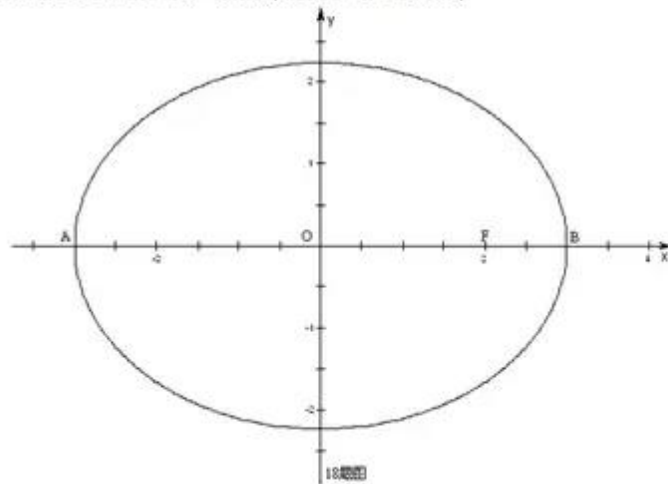
18. (16分) 在平面直角坐标系  $xOy$  中, 如图, 已知椭圆  $\frac{x^2}{9} + \frac{y^2}{5} = 1$  的左右顶点为  $A, B$ , 右焦点为  $F$ , 设过点

$T(t, m)$  的直线  $TA, TB$  与椭圆分别交于点  $M(x_1, y_1), N(x_2, y_2)$ , 其中  $m>0, y_1>0, y_2<0$ .

(1) 设动点  $P$  满足  $PF^2 - PB^2 = 4$ , 求点  $P$  的轨迹

(2) 设  $x_1 = 2, x_2 = \frac{1}{3}$ , 求点  $T$  的坐标

(3) 设  $t=9$ , 求证: 直线  $MN$  必过  $x$  轴上的一点(其坐标与  $m$  无关)



Given an ellipse  $\frac{x^2}{9} + \frac{y^2}{5} = 1$  whose vertices are  $A$  and  $B$  and right focus  $F$ . Suppose that line  $TA$  and line  $TB$  which pass through  $T(t, m)$  intersect the ellipse at  $M(x_1, y_1)$  and  $N(x_2, y_2)$  individually. ( $m>0, y_1>0, y_2<0$ )

1) Moving point P satisfies equation  $PF^2 - PB^2 = 4$ , find the track of P.

2) Assume that  $x_1 = 2$ ,  $x_2 = 1/3$ , find the coordinates of T

3) Assume that  $t = 9$ , prove that line MN must pass through a definite point on the x axis (whose coordinates are independent of m)

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**6.**

Assume a positive sequence  $\{a_n\}$ , whose sum of the first n terms is  $S_n$ , given that  $2a_n = a_1 + a_3$ , sequence  $\{\sqrt{S_n}\}$  is an Arithmetic Sequence with a common difference d.

1) Find the general formula of the sequence  $\{a_n\}$  (in n and d)

2) Assume  $c \in \mathbb{R}$ , for any positive integers m, n and k that satisfy  $m+n=3k$  and  $m \neq n$ , exists equality  $S_m + S_n > cS_k$

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**7.**

Assume sequence  $\{a_n\}$  that satisfies  $|a_n - a_{(n+1)/2}| \leq 1, n \in \mathbb{N}_+$

1) Prove that  $|a_n| \geq 2^{(n-1)}(|a_1| - 2), n \in \mathbb{N}^*$

2) If  $|a_n| \leq (3/2)^n, n \in \mathbb{N}^*$ , prove that  $|a_n| \leq 2, n \in \mathbb{N}^*$

– [2016 Zhejiang Gaokao](#)